## What I should have done to determine the angles of the cuts

8-foot tall triangle with 10 -foot long legs, horizontal ground.


$$
\cos x=\frac{8}{10} \rightarrow x=\cos ^{-1} \frac{8}{10} \approx 37^{\circ}
$$

Keep 37 degrees or cut off 53 degrees. Done. Required knowledge, $10^{\text {th }}$ grade math.
What I spent too long doing to determine the angles of the cuts


8 -foot tall triangle with 10 -foot long legs. The ground is not level, but my iPhone level told me that the slope was 2 degrees down from front to back, so I went with that. I decided to assume that the height of the ground did not vary significantly from the midpoint of the side of the tower to the point below the apex of the $A$.

Law of Sines: $\frac{\sin 88^{\circ}}{x}=\frac{\sin \theta}{96} \rightarrow \theta=\sin ^{-1}\left(\frac{96 \sin 88^{\circ}}{x}\right) \quad$ And also, $\alpha=92-\theta$.
Here is a blown up part of the top end of the left $4 \times 4$ to show what I needed to cut off.

I knew the 3.5 inches from the dimensions of the board and
 that $x+y=120$, the length of the post in inches. I used these two facts to fine the angle ( $\alpha$ ).

$$
\tan \alpha=\frac{3.5}{y}
$$

$$
\begin{gathered}
y=\frac{3.5}{\tan \left(92-\sin ^{-1}\left(\frac{96 \sin 88^{\circ}}{x}\right)\right)} \\
x+y=120 \\
y=120-x
\end{gathered}
$$

$(x, y)$ solved graphically yields $x \approx 115.1, y \approx 4.9$. Then $\alpha=\tan ^{-1} \frac{3.5}{y} \approx 35.5^{\circ}$.

Similar arguments find $\beta$.
Fun exercise for you. Find $\beta$. Let me know what you get!

